

Waves on a rope

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Solution: a. We have,

$$v = \lambda_n f_n = \frac{2L}{n} f_n .$$

Hence, $v_1 = 2L f_1 = 2 \text{ km/s}$.

b. To calculate the frequency, we let,

$$v' = \lambda_3 f_3 = \frac{2L}{3} f_3 .$$

Hence, $f_3 = \frac{3v'_1}{2L} = 3 \text{ kHz}$.

c. We have,

$$v' = \sqrt{\frac{m'g}{\mu}} = \sqrt{2} \sqrt{\frac{mg}{\mu}} = \sqrt{2} v .$$

Hence, $v'_1 = 2.82 \text{ km/s}$.

d. We have,

$$3 = \frac{v'}{v} = \sqrt{\frac{m'g}{\mu} \frac{\mu}{mg}} = \sqrt{\frac{m'}{m}} .$$

Hence, $m' = 9m \approx 9 \text{ kg}$.