Mach-Zehnder and Michelson-interferometer

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Solution: Be $I_0(0,t) = e^{i(kx-\omega t)} = e^{-i\omega t}$ the signal immediately in front of the first beam splitter. Immediately behind it we have two waves $I_{1,2}(0,t) = 2^{-1/2}e^{i(kx-\omega t)} = 2^{-1/2}e^{-i\omega t}$. With the interferometer arm lengths $d_{1,2}$ we have, just in front of the second separator, the signals $I_{1,2}(d_{1,2},t) = 2^{-1/2}e^{i(kd_{1,2}-\omega t)}$. Immediately behind it we have the recombined wave,

$$I_s(t) = 2^{-1/2} e^{i(kd_1 - \omega t)} + 2^{-1/2} e^{i(kd_2 - \omega t)} = 2^{1/2} \cos k(d_1 + d_2) e^{-i\omega t} .$$

That is, after the second beam splitter the signal oscillates with an amplitude that depends on the length difference of the interferometer arms like $\cos k(d_1 + d_2)$.