

## Doppler effect

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**Solution:** a. In the system where the air is at rest the speaker is moving away with the speed  $v$ . Therefore, the frequency that would be perceived by a listener moving along with the wind is,

$$f_{\text{medium}} = \frac{f_0}{1 + v/c} .$$

In the system where the air is at rest the microphone is moving away in the same direction as the speaker with the speed  $u - v < 0$ . Hence,

$$f_{\text{micro}} = f_{\text{medium}} \left( 1 - \frac{u - v}{c} \right) = f_0 \frac{1 - (u - v)/c}{1 + v/c} = f_0 \left( 1 + \frac{-u/c}{1 + v/c} \right) .$$

Alternatively, we calculate the Doppler shift first disregarding the wind,

$$f_{\text{rep}} = f_0 \left( 1 - \frac{u}{c} \right) ,$$

and transforming to the wind system by,  $c \rightarrow c + v$ , giving the same result,

$$f = f_0 \left( 1 - \frac{u}{c + v} \right) .$$

b. (i) With the microphone fixed to the ground  $u = 0$ , we observe  $f = f_0$ .

(ii) In case where the microphone reaches the wind speed,  $u = v$ , we observe  $f = f_0 \frac{1}{1 + v/c}$ , which is the Doppler effect of a moving source.

(iii) Without wind  $v = 0$  but with a microphone velocity  $u$  we observe  $f = f_0 \left( 1 - \frac{u}{c} \right)$ , which is the Doppler of a moving receiver.